

## 1. Coulomb's Law

Coulomb's Law states that the electrostatic force between two **point charges** is:

- Directly proportional to the **product** of the charges.
- Inversely proportional to the **square of the distance** between them.

### Mathematical Expression:

$F = k \frac{q_1 q_2}{r^2}$  where:

- $F$  = Electrostatic force (Newton, **N**)
- $q_1, q_2$  = Magnitudes of charges (Coulomb, **C**)
- $r$  = Distance between charges (meters, **m**)
- $k$  = Coulomb's constant ( $9 \times 10^9 \text{ Nm}^2/\text{C}^2$ ) in vacuum

### Key Points:

- Like charges repel, unlike charges attract.
- Force is along the line joining the charges.
- Works best for point charges or spherical distributions.
- Medium affects force: Different materials reduce or enhance electrostatic force.

## 2. Significance of Medium in Coulomb's Law

The medium between charges affects the force due to its **dielectric constant** ( $\epsilon_r$ ).

$$F_{\text{medium}} = \frac{1}{4\pi\epsilon_0\epsilon_r} \times \frac{q_1 q_2}{r^2}$$

where  $\epsilon_r$  is the **relative permittivity** (dielectric constant) of the medium.

### How Medium Affects Electrostatic Force?

- Vacuum/Air:  $\epsilon_r = 1$ , maximum force.
- Water:  $\epsilon_r = 80$ , force is reduced by 80 times.
- Glass:  $\epsilon_r = 4 - 10$ , moderate force reduction.
- Metals:  $\epsilon_r \rightarrow \infty$ , force inside conductors is nearly zero (shielding effect).

♦ Higher dielectric constant → Weaker electrostatic force. ♦ This principle is used in capacitors and insulation materials.

### 3. Understanding Dielectric Constant in Simple Terms

Think of **dielectric constant** as how much a material weakens the force between charges.

- **Vacuum/Air** ( $\epsilon_r = 1$ ) → No weakening, full force.
- **Water** ( $\epsilon_r = 80$ ) → Weakens force by 80 times.
- **Glass** ( $\epsilon_r \approx 4 - 10$ ) → Weakens force moderately.
- **Metals** ( $\epsilon_r \rightarrow \infty$ ) → Force is almost zero (used for shielding, e.g., Faraday cage).

#### ✦ Analogy:

- Talking in an **empty room** (vacuum) = voice is clear.
- Talking in a **crowded room** (water) = voice is weak.
- Talking in a **semi-crowded room** (glass) = voice is reduced, but not completely.

**In summary, dielectric constant = how much a material reduces electrostatic force.**

#### 4. Theory of Quantization of Charge

The **quantization of charge** means that charge always exists in discrete multiples of the elementary charge 'e' ( $1.6 \times 10^{-19}$  C).

**Formula:**

$Q = n \times e$  where:

- $Q$  = total charge,
- $n$  = integer ( $\pm 1, \pm 2, \pm 3 \dots$ )
- $e$  = charge of an electron ( $1.6 \times 10^{-19}$  C)

♦ No fraction of charge can exist. ♦ Every charge in the universe is a whole-number multiple of this fundamental charge. ♦ Example: If a body has a charge of  $-3e$ , it means it has an excess of 3 electrons.

#### 5. Quiz Time! 📄

**MCQs on Coulomb's Law:**

1. Coulomb's Law is applicable to: a) Only small charged bodies b) Only neutral bodies c) Point charges at rest d) Moving charges
2. The force between two charges is **inversely proportional to**: a) Product of charges b) Distance between them c) Square of the distance between them d) Medium's dielectric constant
3. If the distance between two charges is **tripled**, the force becomes: a) 9 times stronger b) 9 times weaker c) 3 times stronger d) 3 times weaker

**Fill in the Blanks:**

1. The SI unit of charge is \_\_\_\_\_.
2. Coulomb's Law states that the force between charges is \_\_\_\_\_ **proportional** to the square of their separation.
3. In vacuum, the value of Coulomb's constant is \_\_\_\_\_  $\text{Nm}^2/\text{C}^2$ .
4. The force between two charges in water is \_\_\_\_\_ **times weaker** than in air.
5. The charge of a proton is \_\_\_\_\_ C.

**Match the Following:**

Column A	Column B
Coulomb's Law	Electrostatic Force
Dielectric Constant	Reduces force between charges
Charge Quantization	Discrete multiples of e
Force between two charges	Inversely proportional to distance squared
Vacuum permittivity	$8.85 \times 10^{-12} \text{ C}^2/\text{Nm}^2$

 Now, complete your assignment! 😊 ⚡

### **Example**

Two 0.5 kg spheres are placed 25 cm apart. Each sphere has a charge of 100  $\mu\text{C}$ , one of them positive and the other negative. Calculate the electrostatic force between them, and compare it to their weight.

$$\text{Coulomb's Law: } |F| = \frac{k |q_1| |q_2|}{r^2} \quad k = 9 \times 10^9 \text{ N m}^2 \text{ C}^{-2}$$

$$|q_1| = |q_2| = 100 \mu\text{C} = 100 \times 10^{-6} \text{ C} = 10^{-4} \text{ C}$$

$$r = 25 \text{ cm} = 0.25 \text{ m}$$

$$F_{\text{electrostatic}} = \frac{9 \times 10^9 \times 10^{-4} \times 10^{-4}}{0.25^2} = 1440 \text{ N}$$

$$F_{\text{weight}} = mg = 0.5 \times 9.8 = 4.9 \text{ N}$$

# Electrostatic force

- The electrostatic force is a **vector**, written  $\vec{F}$
- Vectors have a **magnitude** and a **direction**. This may be indicated by **components**  $\vec{F} = (F_x, F_y, F_z)$
- The **magnitude** is sometimes written as  $|\vec{F}|$ . It can be evaluated as  $|\vec{F}| = \sqrt{F_x^2 + F_y^2 + F_z^2}$
- The **direction** can be indicated by a unit vector